

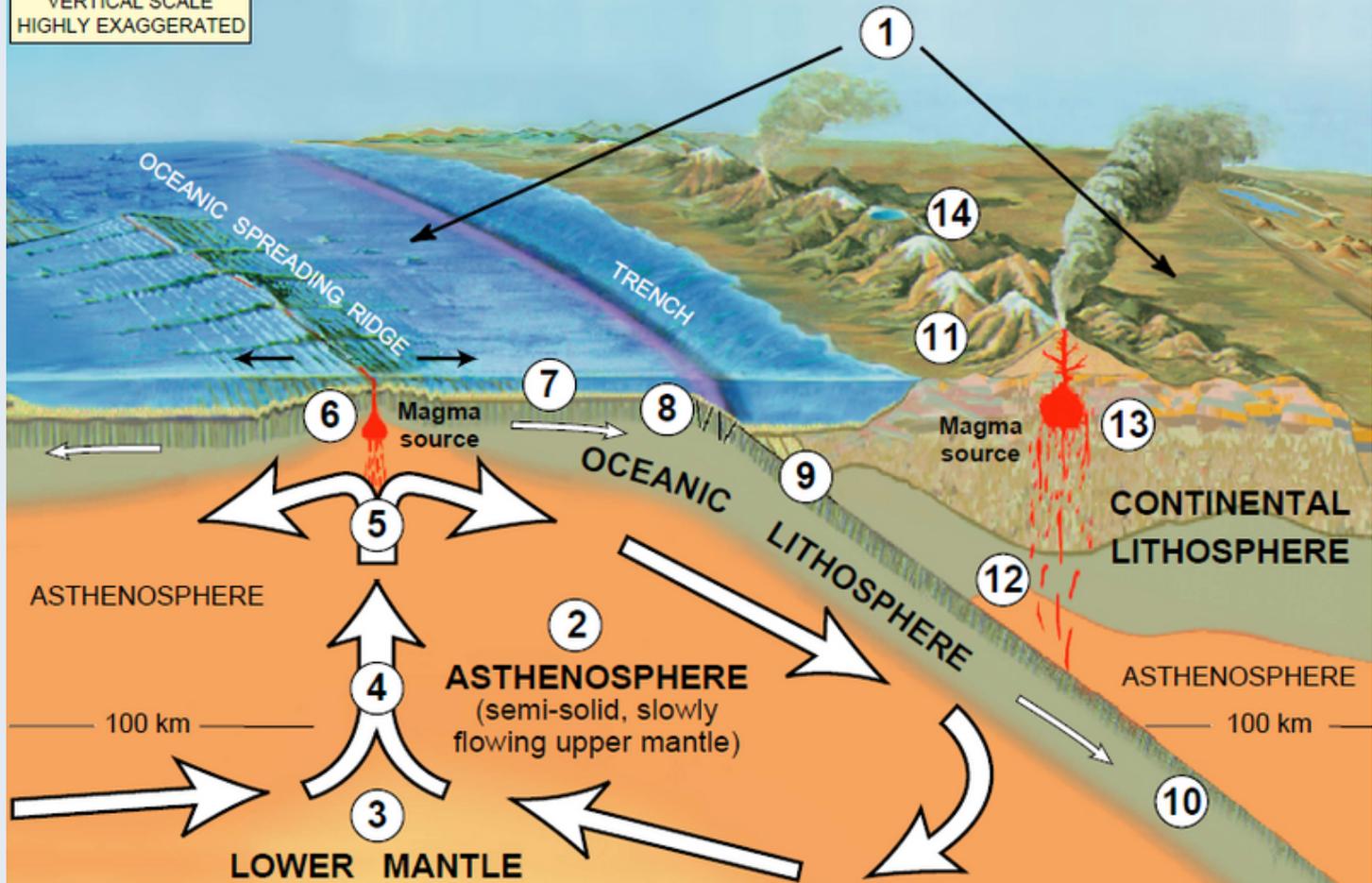


THANKSGIVING

LAKE/OCEAN LOADING FLEXURE

Beineng ZHANG, SIO 234, NOV-23-2016

VERTICAL SCALE
HIGHLY EXAGGERATED



<http://volcanoes.usgs.gov/about/edu/dynamicplanet/nutshell.php>

WHY INVESTIGATING LAKE/OCEAN LOADING

Apart from tectonic loading, other sources may also alter the state of stress of plates, thus contributing to the modulation of earthquake cycles.

LAKE LOADING

Modulation of the earthquake cycle at the southern San Andreas fault by lake loading
(Luttrell et al. , 2007)

REGION OF INTEREST

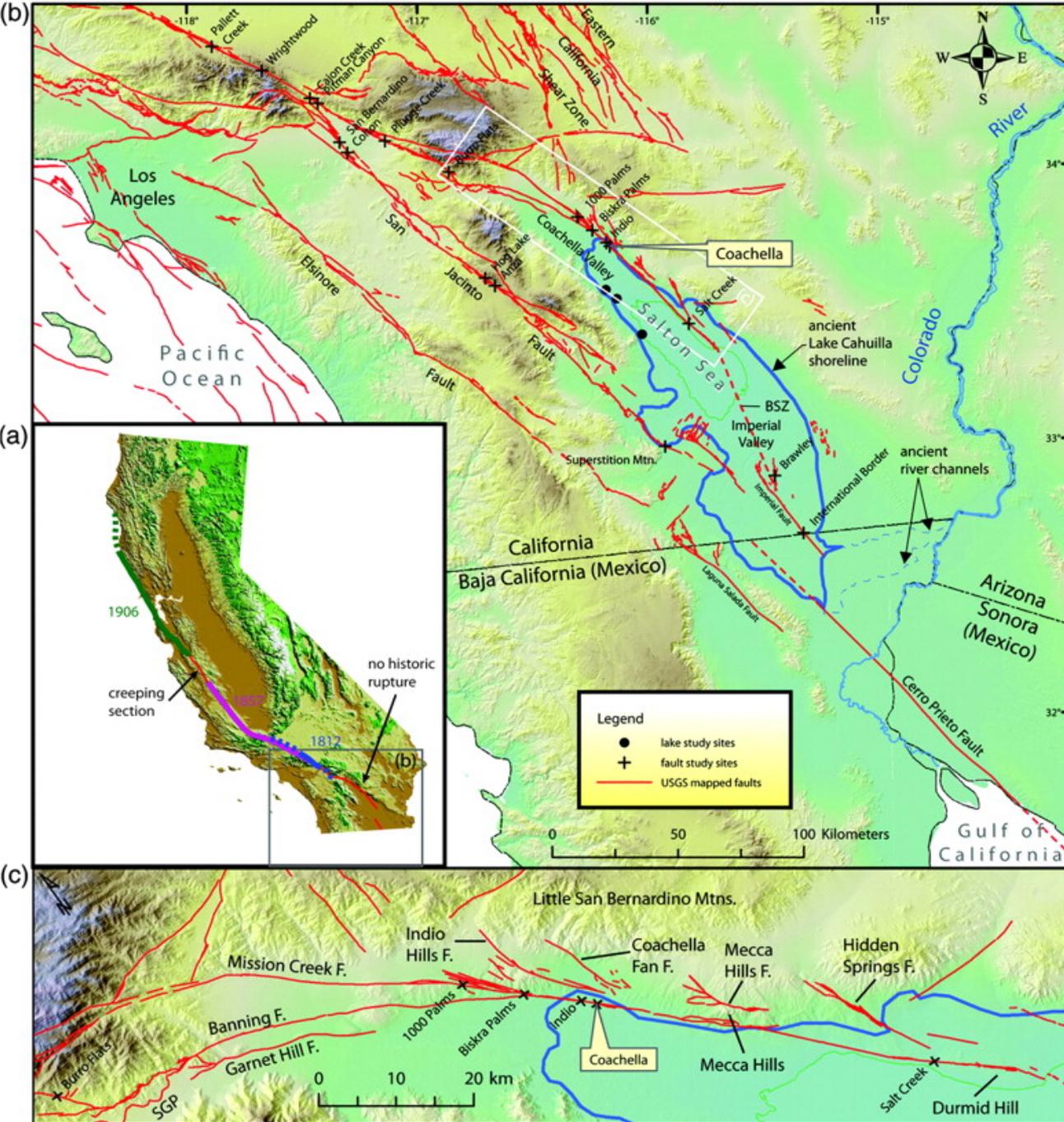
SALTON

TROUGH

Active Fault System:
San Andreas Fault
San Jacinto Fault,
Imperial Fault

Potential to produce
large earthquakes,
but no major ruptures
on SAF and SJF for
the past 300 year

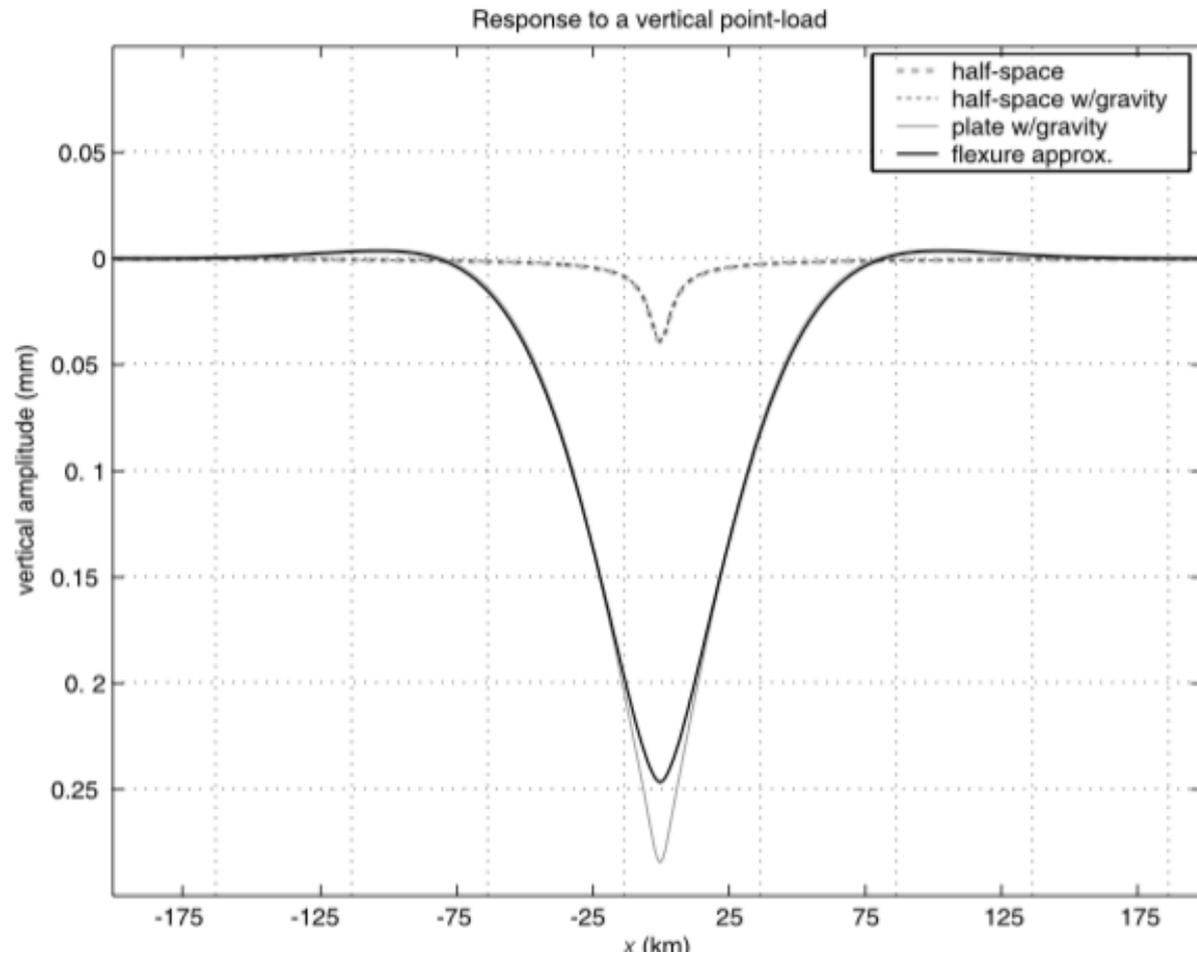
Philibisian et al. (2011)



MODEL

- A Thick Elastic Plate Overlaying a Viscoelastic Half-Space
- Coulomb Stress (Readiness to Rupture)
$$\sigma_c = \sigma_s - \mu_f \sigma_n$$
- Change in Normal Stress Due to Lake Level Changes
 1. Lithosphere Bending
 2. Pore Pressure (decrease normal stress)

Smith and Sandwell
(2004)



A Thick Elastic Plate Overlaying a Viscoelastic Half-Space

Short-term: Viscoelastic half-space dominates.

Long-term: Elastic plate dominates.

SOLUTION of a Thin Elastic Plate

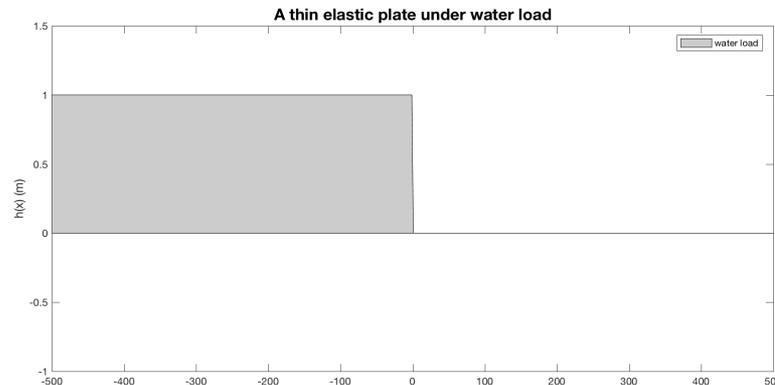
- Convolve the line-load solution with lake load expression

$$u(x) = \int_{-\infty}^{\infty} w(x') f(x - x') dx'$$

Where

$$w(x) = \frac{V_o \alpha^3}{8D} e^{-\frac{x}{\alpha}} \left(\cos \frac{x}{\alpha} + \sin \frac{x}{\alpha} \right)$$

(Turcott&Schubert 3.130)



Flexural Parameter

$$\alpha = \left[\frac{4D}{(\rho_m - \rho_w)g} \right]^{\frac{1}{4}}$$

Flexural Rigidity

$$D = \frac{Eh^3}{12(1 - \nu^2)}$$

Heaviside(Step) Function

$$H(x) = 1 \text{ for } x \geq 0$$

Lake load

$$f(x) = 1 - H(x)$$

DERIVATION(1)

$$\begin{aligned}u(x) &= \int_{-\infty}^{\infty} w(x') f(x - x') dx' \\ &= \int_{-\infty}^{\infty} w(x') [1 - H(x - x')] dx'\end{aligned}$$

Expect Odd Function. Consider Half-Space.

$$u(x) = \int_0^{\infty} w(x') [1 - H(x - x')] dx'$$

Where

$$x < x' \quad 1 - H(x - x') = 1$$

$$x \geq x' \quad 1 - H(x - x') = 0$$

DERIVATION(2)

$$\begin{aligned}u(x) &= \int_0^x w(x') dx' \\ &= \frac{V_o \alpha^3}{8D} \int_0^x e^{-\frac{x'}{\alpha}} \left(\cos \frac{x'}{\alpha} + \sin \frac{x'}{\alpha} \right) dx'\end{aligned}$$

Integration by Parts

$$\int e^{-\frac{x}{\alpha}} \sin \frac{x}{\alpha} dx$$
$$j = e^{-\frac{x}{\alpha}} \quad dk = \sin \frac{x}{\alpha} dx$$
$$dj = -\frac{1}{\alpha} e^{-\frac{x}{\alpha}} dx \quad k = -\alpha \cos \frac{x}{\alpha}$$

$$\int e^{-\frac{x}{\alpha}} \sin \frac{x}{\alpha} dx = -\alpha e^{-\frac{x}{\alpha}} \cos \frac{x}{\alpha} - \int e^{-\frac{x}{\alpha}} \cos \frac{x}{\alpha} dx$$

FINAL EXPRESSION

The result yields

$$u(x) = \frac{V_o \alpha^3}{8D} \left[-\alpha e^{-\frac{x'}{\alpha}} \cos \frac{x'}{\alpha} \right] \Big|_0^x$$

$$u(x) = \frac{V_o \alpha^4}{8D} \left(1 - e^{-\frac{x}{\alpha}} \cos \frac{x}{\alpha} \right)$$

Solution of Lithosphere Bending Under Lake Load

$$u(x) = \frac{V_o \alpha^4}{8D} \left(1 - e^{-\frac{|x|}{\alpha}} \cos \frac{|x|}{\alpha} \right) \text{sign}(x)$$

NORMAL STRESS

$$\epsilon_{xx} = -z_o \frac{d^2 u}{dx^2}$$
$$\sigma_{xx} = \frac{E}{1 - \nu^2} \epsilon_{xx}$$

$$\sigma_{xx} = \frac{3V_o \alpha^2}{H^2} \left(\frac{z_o}{H} \right) e^{-\frac{|x|}{\alpha}} \sin \frac{|x|}{\alpha} \text{sign}(x)$$

Values Chosen

Young's Modulus

$$E = 70 \text{ GPa}$$

Poisson's Ratio

$$\nu = 0.25$$

Plate Thickness

$$H = 30 \text{ km}$$

Seismogenic Depth

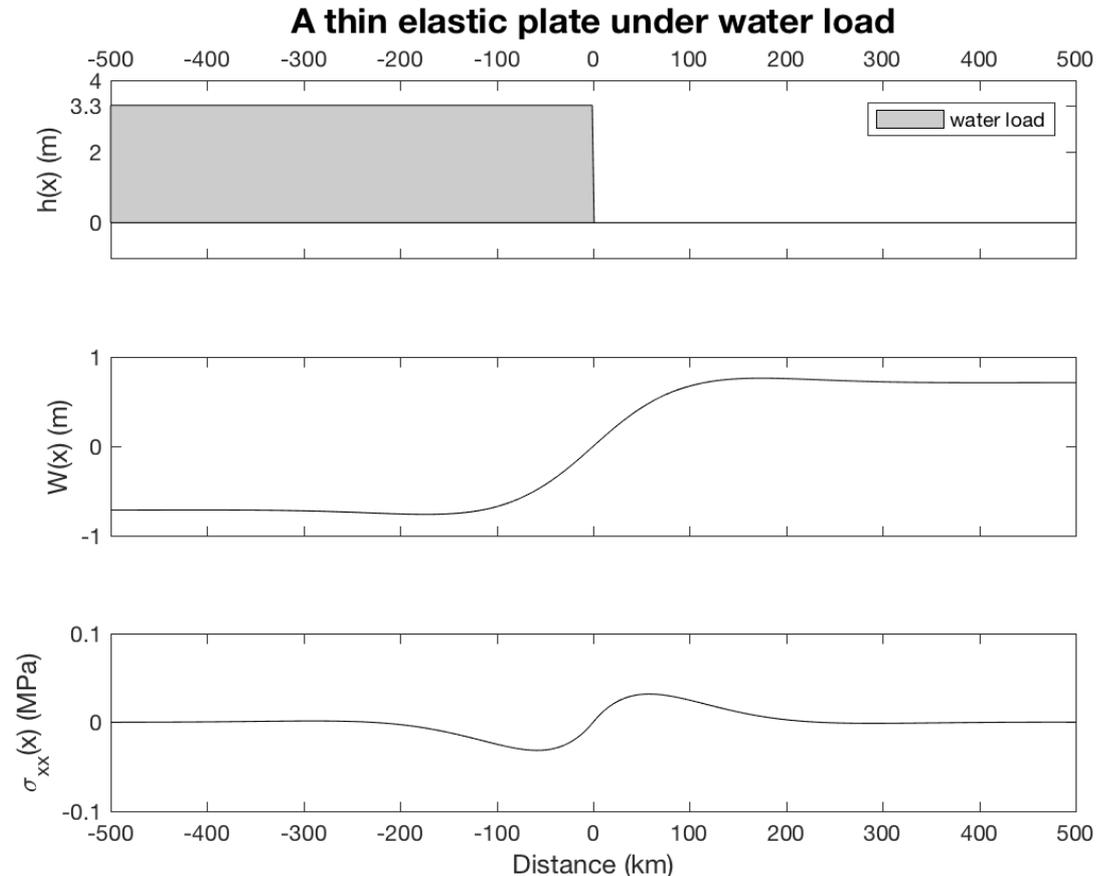
$$z_o = 5 \text{ km}$$

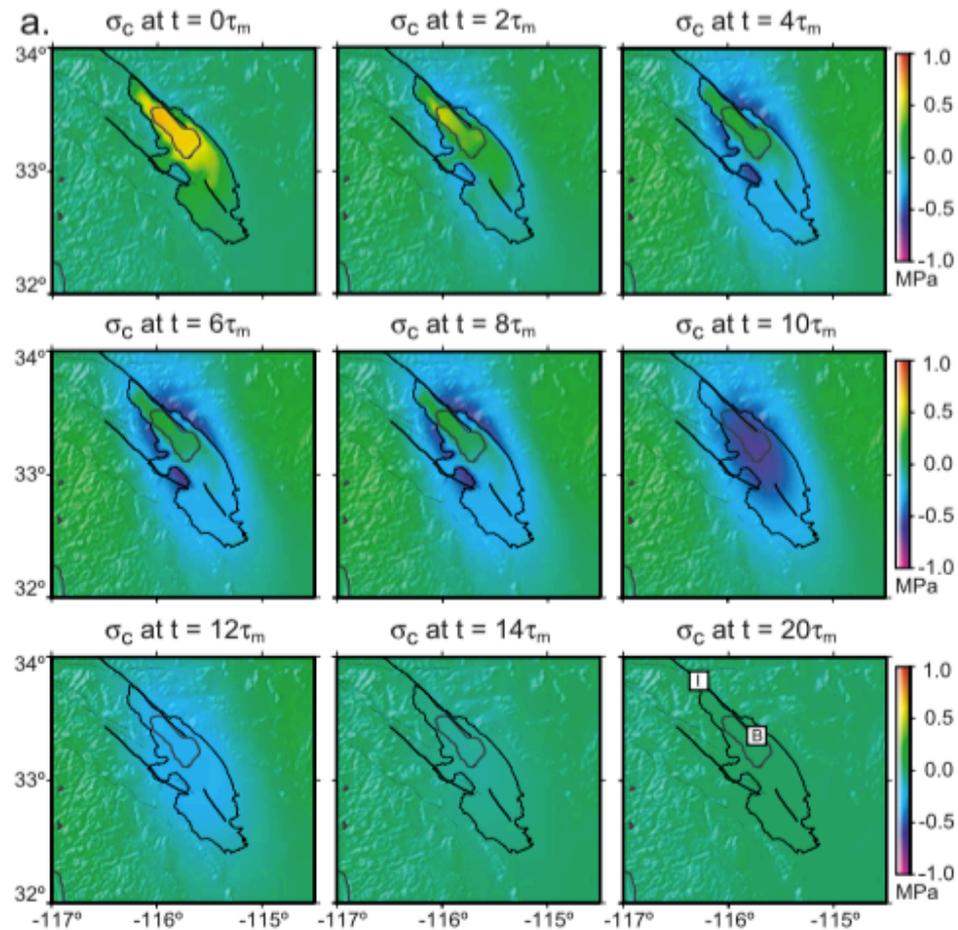
Line Load

$$V_o = \rho_w g h$$

A Thin Plate at Water Depth = 3.3km

Without effect from pore pressure, the plate experiences compressional deformation in the lake and tensile deformation outside.

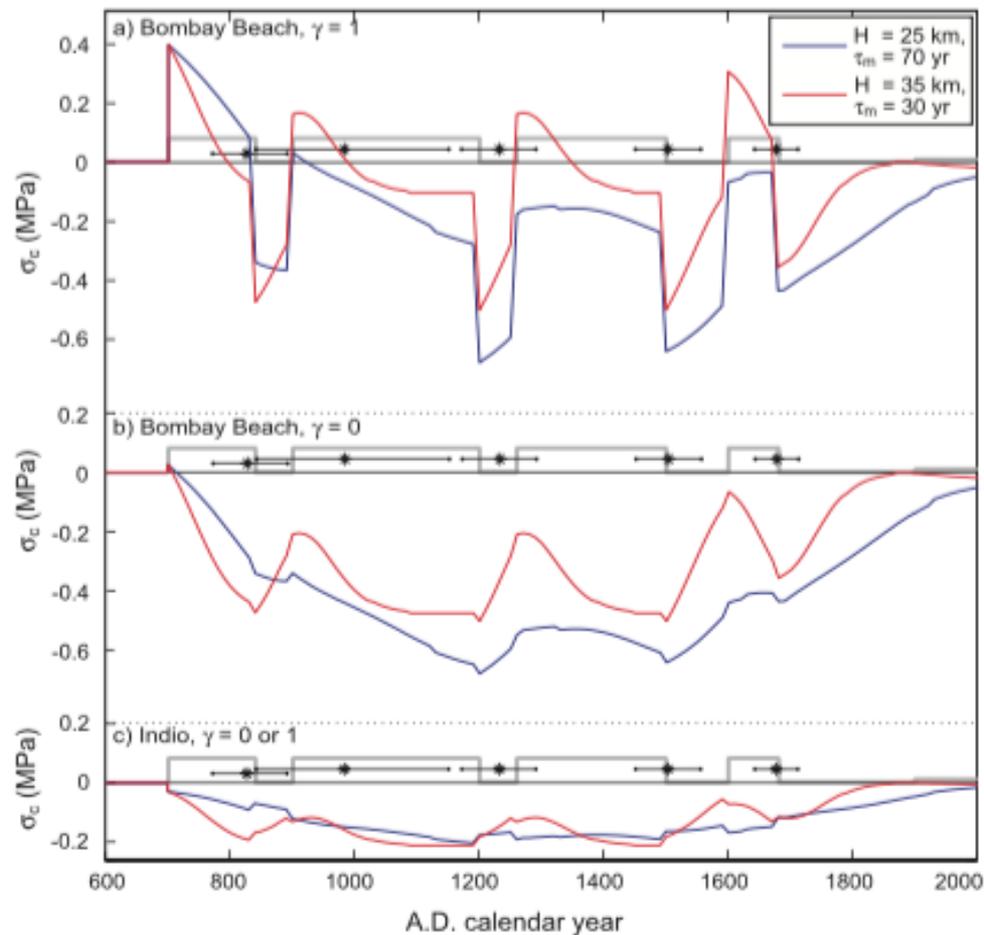




Luttrell et al. (2007)

Stress Field Over Time

Coulomb stress perturbations due to a single cycle of lake formation and desiccation. The lake fills at $0\tau_m$, remains full, and falls at $10\tau_m$. Negative Coulomb stress decreases the likeliness of rupture.



Luttrell et al. (2007)

Coulomb Stress vs. Earthquake Cycle

2 Best Fitting Models ($H=25\text{km}$, $\text{Tau}=70\text{yr}$) and ($H=35\text{km}$, $\text{Tau}=30\text{yr}$)

Perturbation 0.2–0.6 MPa within the lake and 0.1–0.2 MPa outside the lake

An order of magnitude smaller than Coulomb stress associated with tectonic loading. (Therefore lake perturbations are likely to modulate the earthquake cycle only when faults are near critically stressed.)

OCEAN LOADING

Ocean loading effects on stress at near shore plate boundary fault systems

Luttrel and Sandwell (2010)

THANK YOU

