#### http://topex.ucsd.edu/gmtsar/tar/GMTSAR\_2ND\_TEX.pdf

#### **GMTSAR:**

An InSAR Processing System Based on Generic Mapping Tools

(Second Edition)

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May 1, 2011; Revised: June 1, 2016

InSAR Workshop, August 08-10 in this room, no cost.

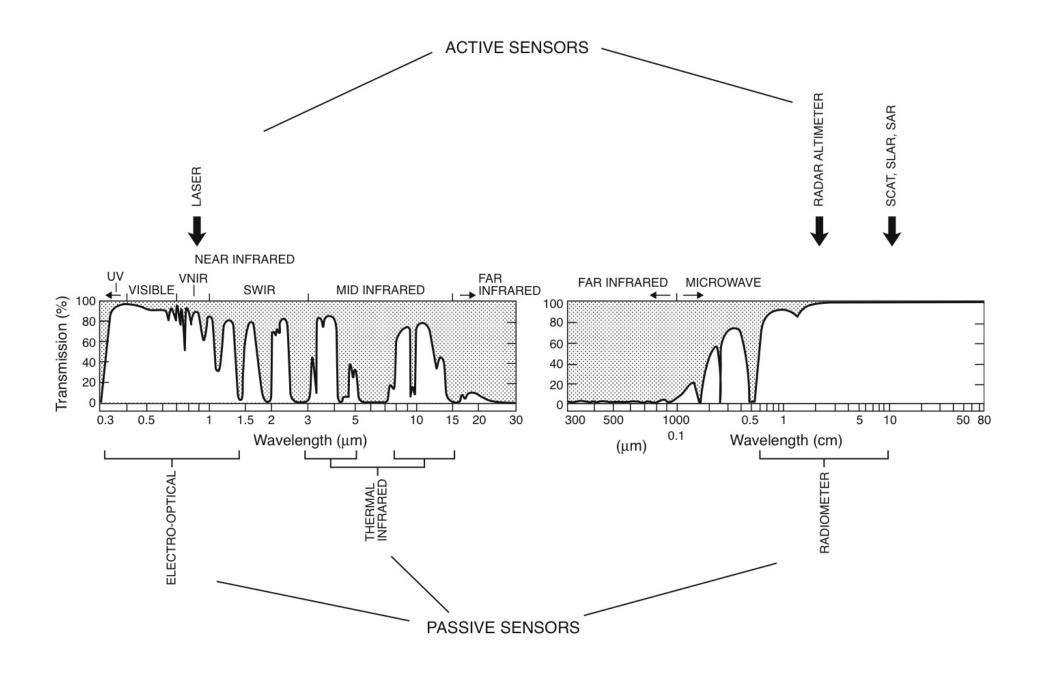
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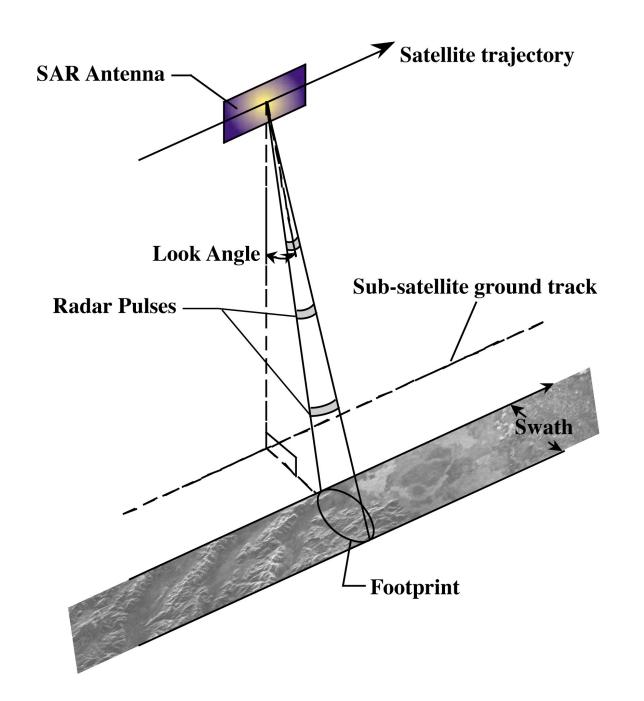
http://www.unavco.org/education/professional-development/short-courses/2018/insar-gmtsar/insar-gmtsar.html (closed now so send me an e-mail <u>dsandwell@ucsd.edu</u>)

#### **Contents**

| 1 | Introduction  1.1 Objectives and limitations of GMTSAR  1.2 Algorithms: SAR, InSAR, and the need for precise orbits  1.2.1 Proper focus  1.2.2 Transformation from geographic to radar coordinates  1.2.3 Image alignment  1.2.4 Flattening interferogram - no trend removal | 5<br>5<br>6<br>7<br>8<br>9<br>10                               |
|---|--|--|
| 2 | Software 2.1 Standard Products   | 11<br>11<br>12   |
| 3 | Processing Examples 3.1 Two-pass processing  | 14<br>15<br>18<br>26   |
| 4 | Problems   | 32   |
| A | Principles of Synthetic Aperture Radar  A.1 Introduction   | 33<br>33<br>34<br>37<br>38<br>39<br>40<br>40<br>40<br>40<br>42 |
| B | SAR Image Formation  B.1 Overview of the range-doppler algorithm  B.2 Processing on board the satellite  B.3 Digital SAR processing  B.4 Range compression  B.5 Azimuth compression  B.6 Example with ALOS L-band orbit  B.7 Problems  InSAR  C.1 Forming an interferogram   | 44<br>44<br>45<br>49<br>51<br>58<br>61<br>62                   |
|   | C.2 Contributions to Phase  C.3 Phase due to earth curvature  C.4 Look angle and incidence angle for a spherical earth  C.5 Critical baseline  | 63<br>64<br>65<br>67   |

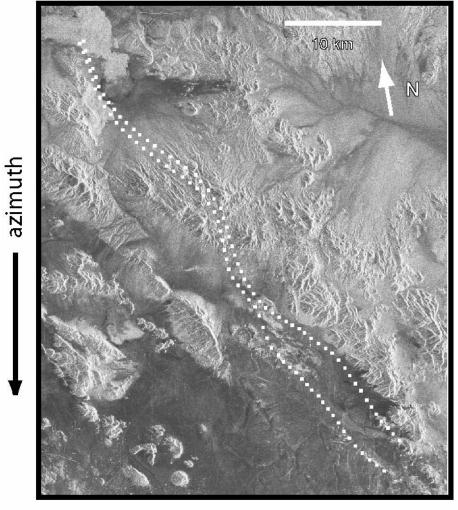
|   | C.6   | Persistent point scatterer and critical baseline                | 68  |
|---|-------|---|-----|
|   | C.7   | Phase due to topography   | 69  |
|   | C.8   | Altitude of ambiguity   | 70  |
|   | C.9   | Phase due to earth curvature and topography – exact formula     | 70  |
|   | C.10  | Problems  | 74  |
| D | Scan  | SAR Processing and Interferometry                               | 75  |
|   | D.1   | Problems  | 80  |
| E | Sent  | inel TOPS-mode processing and interferometry                    | 81  |
|   | E.1   | Introduction  | 81  |
|   | E.2   | Traditional Image Alignment Fails with TOPS-Mode Data           | 83  |
|   | E.3   | Geometric Image Registration                                    | 84  |
|   | E.4   | Enhanced Spectral Diversity                                     | 86  |
|   | E.5   | Elevation Antenna Pattern (EAP) Correction (IPF version change) | 87  |
|   | E.6   | Examples of TOPS Interferogram processing                       | 87  |
|   | E.7   | Processing setup and commands:                                  | 97  |
|   | E.8   | Problems  | 99  |
| F | Geol  | location accuracy for Pinon corner reflectors                   | 100 |
| G | Insta | allation of GMTSAR  | 107 |



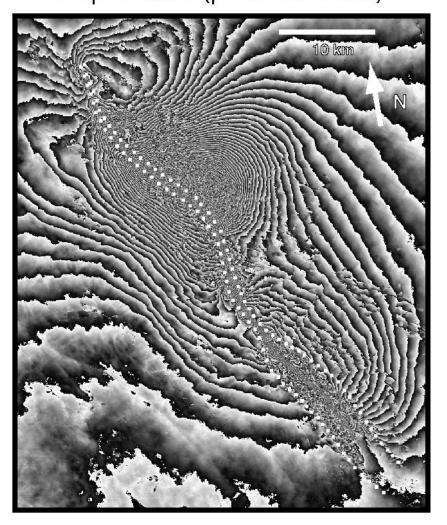


## amplitude and phase

step 1 - SAR (amplitude)

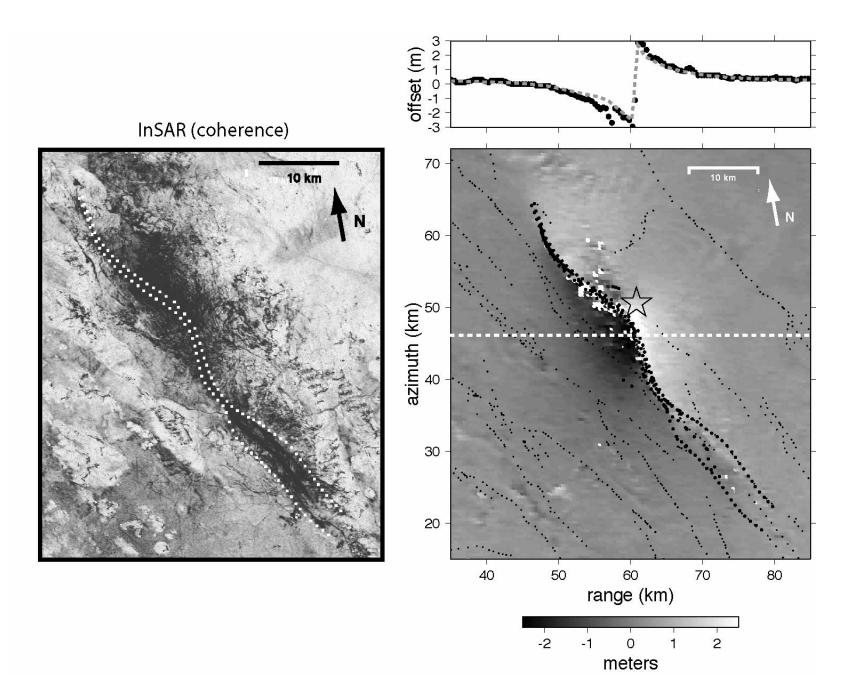


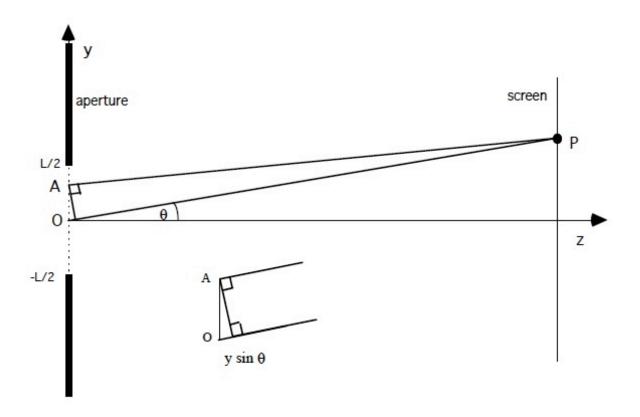
step 2 - InSAR (phase difference)



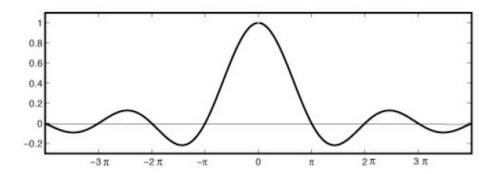
range

## coherence and pixel matching



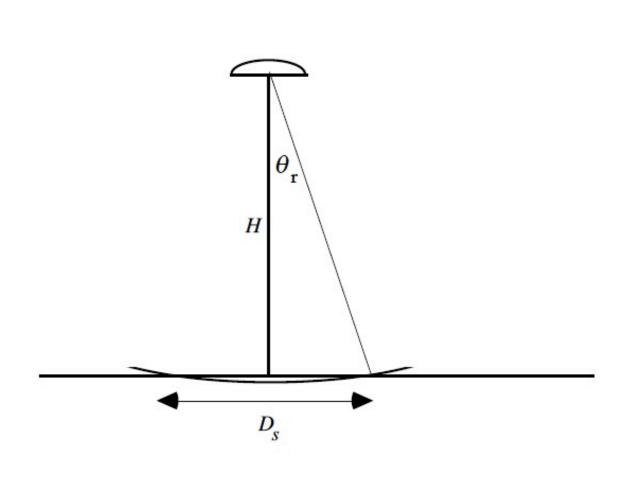


The illumination pattern on the screen is shown in the following diagram.



The first zero crossing, or angular resolution  $\theta_r$  of the sinc function occurs when the argument is  $\pi$  so  $\sin\theta_r = \frac{\lambda}{L}$  and for small angles  $\theta_r \cong \lambda/L$  and  $\tan\theta_r \cong \sin\theta_r$ . Note that

## resolution: optical vs. microwave



$$D_s = 2H\sin\theta_r = 2H\frac{\lambda}{L}$$

$$H = 800 km$$
.

#### Optical:

$$L = 1m$$

$$\lambda = 0.5 \mu m$$

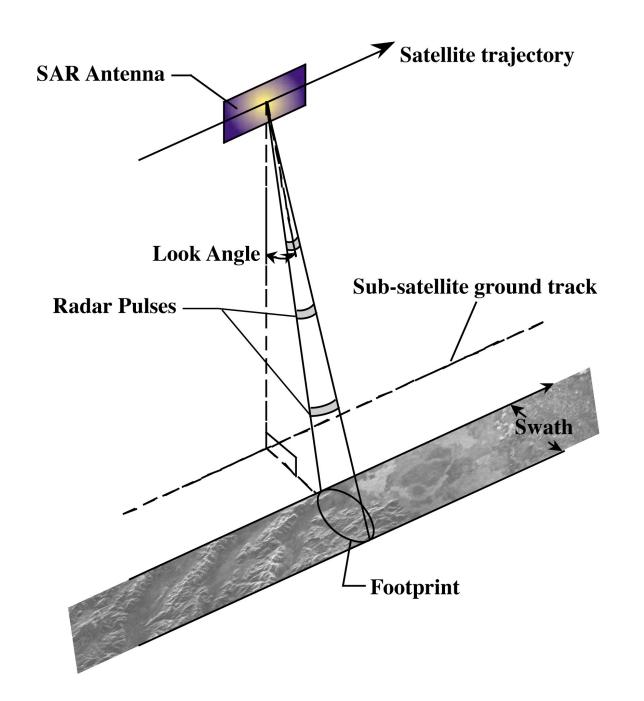
$$D_s = 0.8m$$

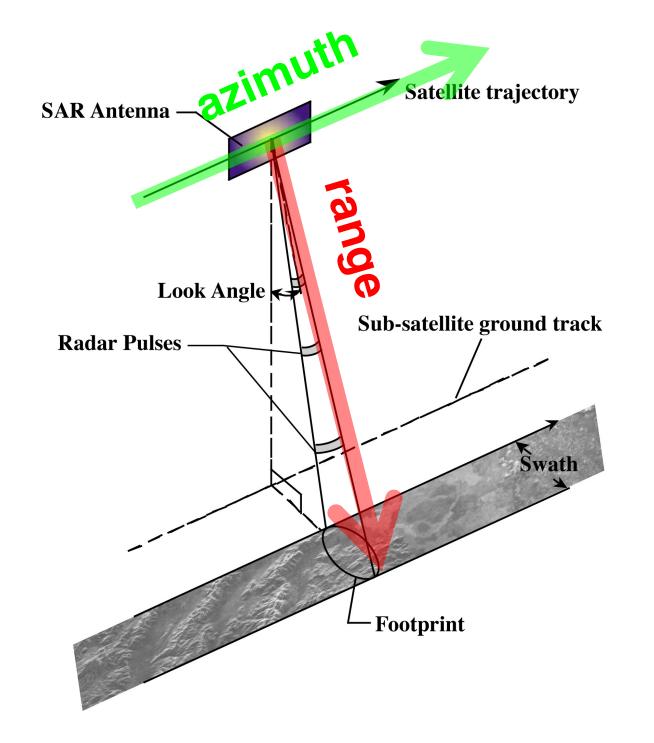
#### *Microwave*:

$$L = 10m$$

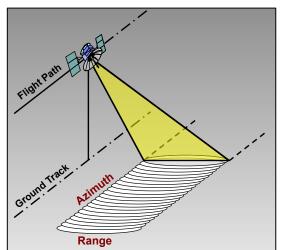
$$\lambda = 0.23m$$

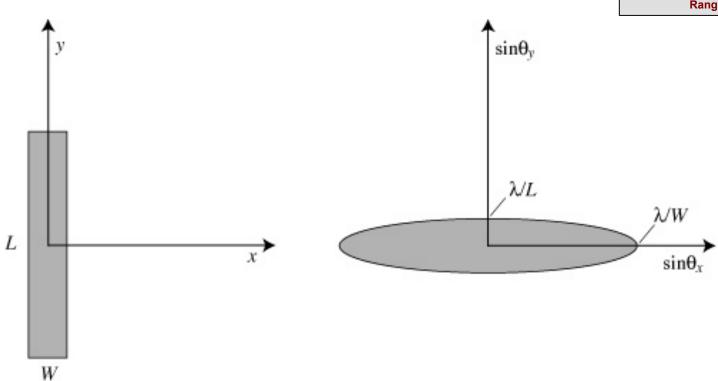
$$D_s = 46,000m!!!!!!$$





## 2-D Aperture



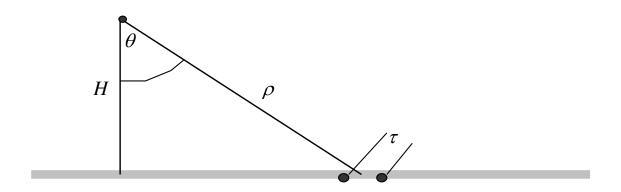


$$P(\theta_{x}, \theta_{y}) = \int_{-L/2}^{L/2} \int_{-W/2}^{W/2} A(x, y) \exp\left[i\frac{2\pi}{\lambda} \left(x \sin \theta_{x} + y \sin \theta_{y}\right)\right] dxdy$$

$$P(\theta_{x}, \theta_{y}) = LW \operatorname{sinc}\left(\frac{\pi W \sin \theta_{x}}{\lambda}\right) \operatorname{sinc}\left(\frac{\pi L \sin \theta_{y}}{\lambda}\right)$$

## Notes on BB

## range resolution



 $\theta$  - look angle

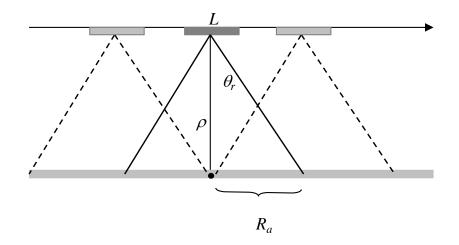
H - spacecraft height

 $\tau$  - pulse length

C - speed of light

$$R_r = \frac{C\tau}{2\sin\theta}$$

## azimuth resolution



L - length of radar antenna

 $\rho$  - nominal slant range  $H/\cos\theta$ 

 $\lambda$  – wavelength of radar

unfocussed

$$R_a = \rho \sin \theta_r = \rho \lambda / L$$

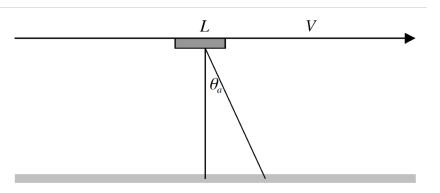
focussed

$$R_a' = \frac{\lambda H}{2R_a \cos \theta} = \frac{L}{2}$$

#### **Pulse Repetition Frequency**

#### **Minimum PRF (Lower Bound)**

- PRF needs to be high enough to sample the entire Doppler spectrum to avoid aliasing
- PRF defines the Nyquist frequency
- Maximum Doppler shift must be less than the Nyquist

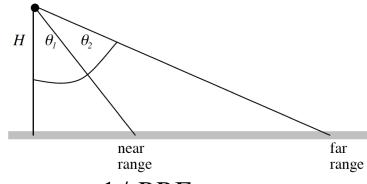


$$\frac{\Delta f}{f_0} = \frac{V \sin \theta_a}{c} \Rightarrow \Delta f = \frac{V}{L}$$

$$PRF > 2\Delta f = \frac{2V}{L}$$

#### **Maximum PRF (Upper Bound)**

 Echo from far range of first pulse must return before the echo from near range of second pulse

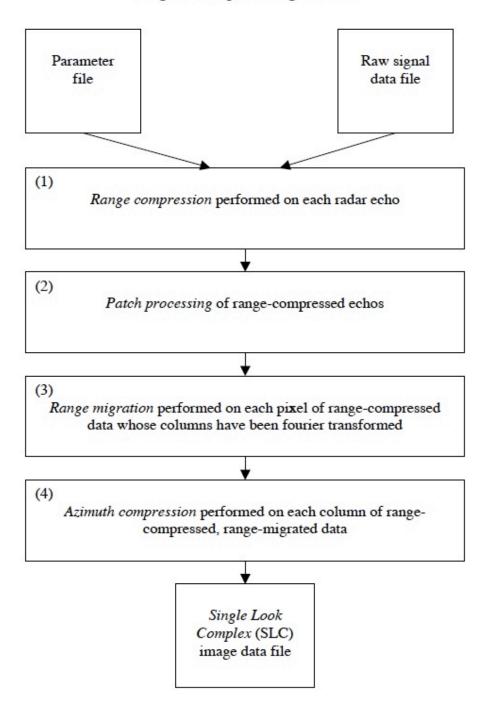


$$t_2 < t_1 + 1 / PRF \Rightarrow$$

$$PRF < \frac{c}{2H} \left( \sec \theta_2 - \sec \theta_1 \right)^{-1}$$

## **SAR** processor

Digital SAR processing overview



## amplitude image



1) This is an image of radar backscatter from a stack of ERS SAR data. The flight path is top to bottom and the radar looks from the right. The area is the Salton Sea and Cochella Valley, and the tic marks are spaced at 10 km. The satellite is 7159717m from the center of the Earth, the local Earth radius is 6371593 m, and the range to the center of the image is 850148 m. Calculate the look angle to the center of the image. Identify areas of layover. What is the minimum mountain slope in the areas of layover? Why is the Salton Sea dark'

## zoom of amplitude image



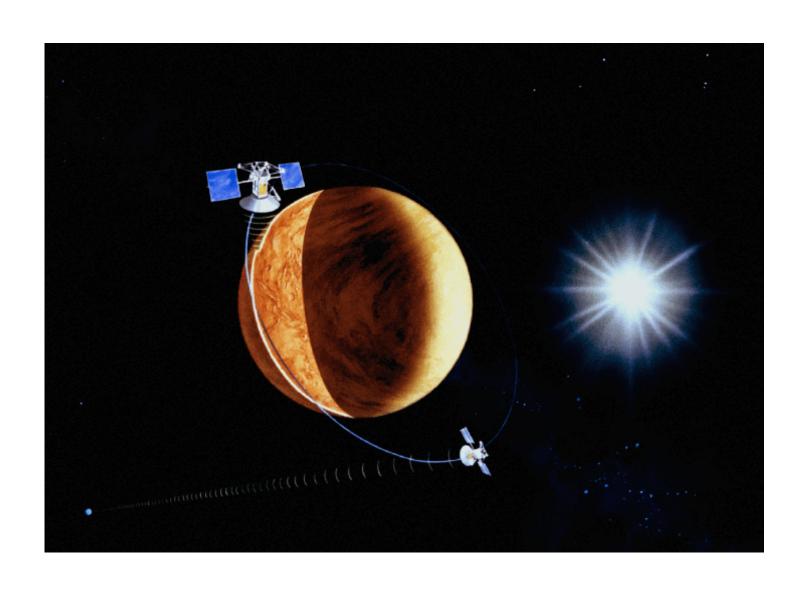
2) This is a zoom of the previous image with 5 km tic marks. Use a map to identify each of the three curved lines running through the images. Why do the fields have different backscatter? Why aren't the fields exactly square? Why do the bright spots have cross patterns?

# Magellen SAR

1990-1994

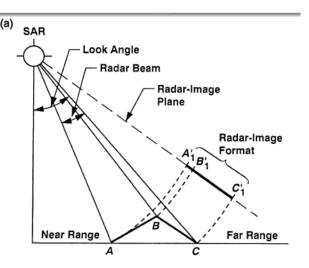


# Magellen SAR 1990-1994

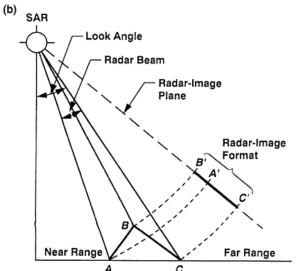


## geometry

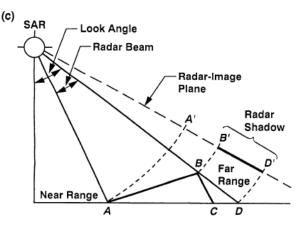
### foreshortening

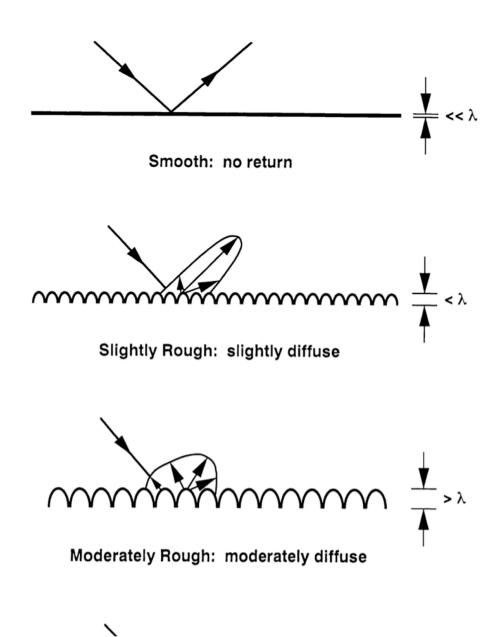


layover



shadowing





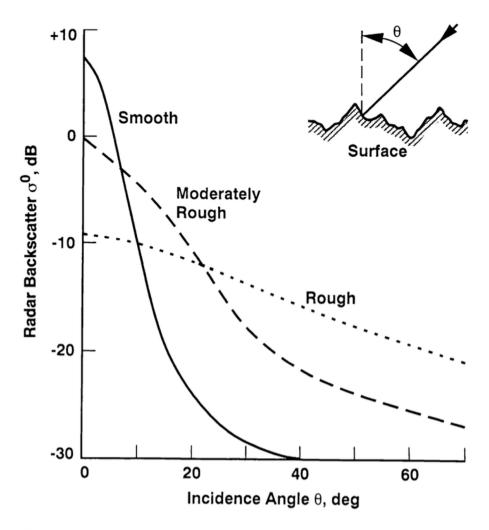
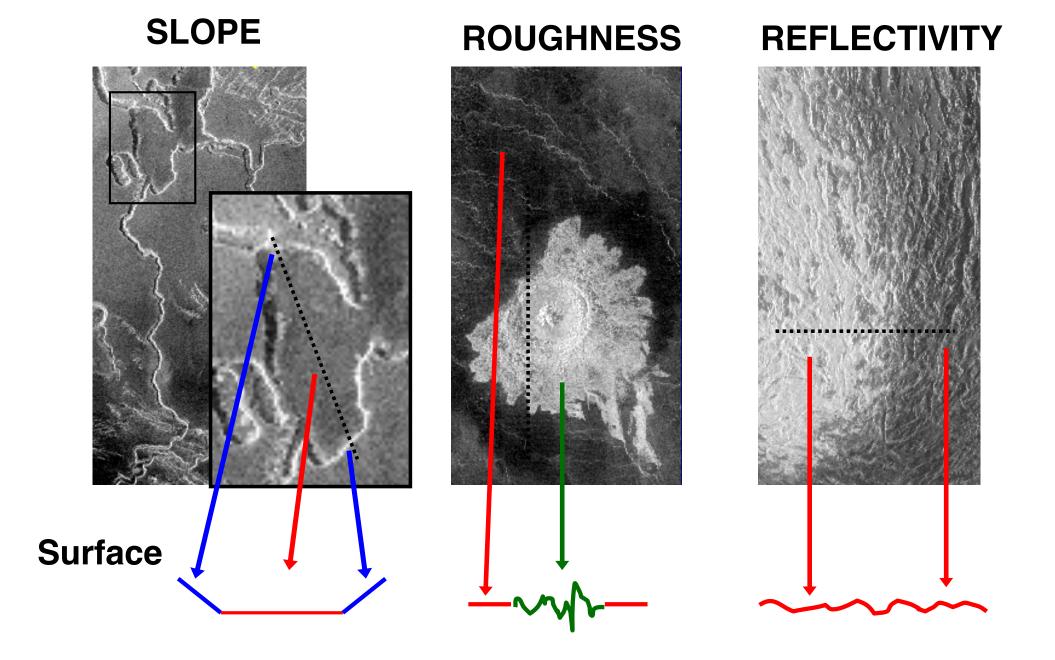


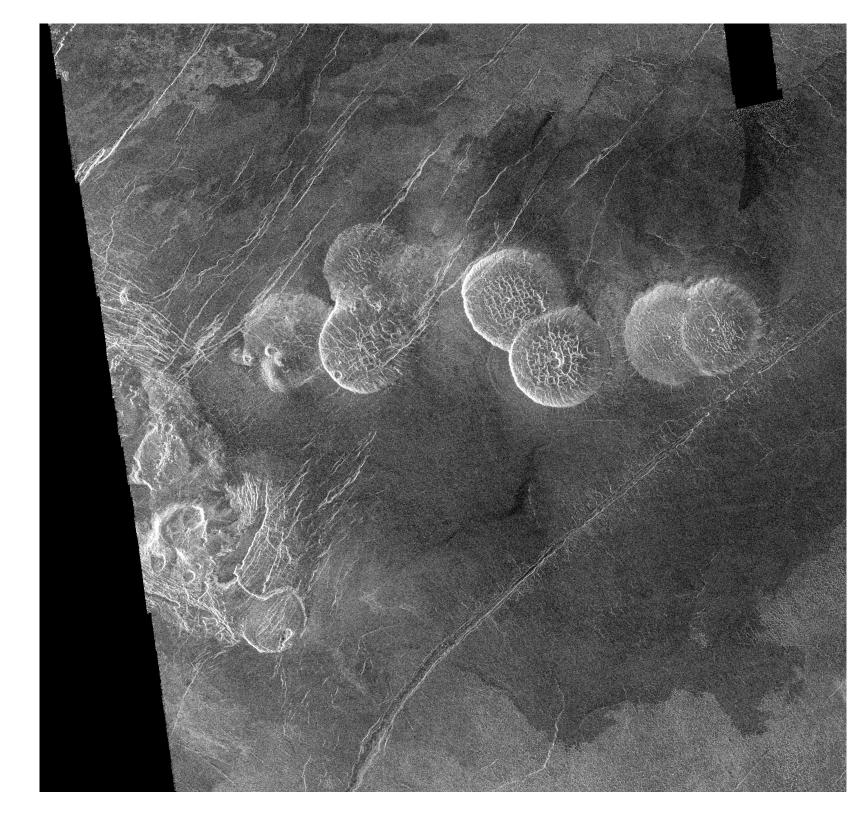
Figure 5-9. Radar backscatter as a function of incidence angle for representative surfaces. For angles less than about 25 deg, smoother surfaces have greater backscatter than rougher surfaces.

# **Radar Image Properties**



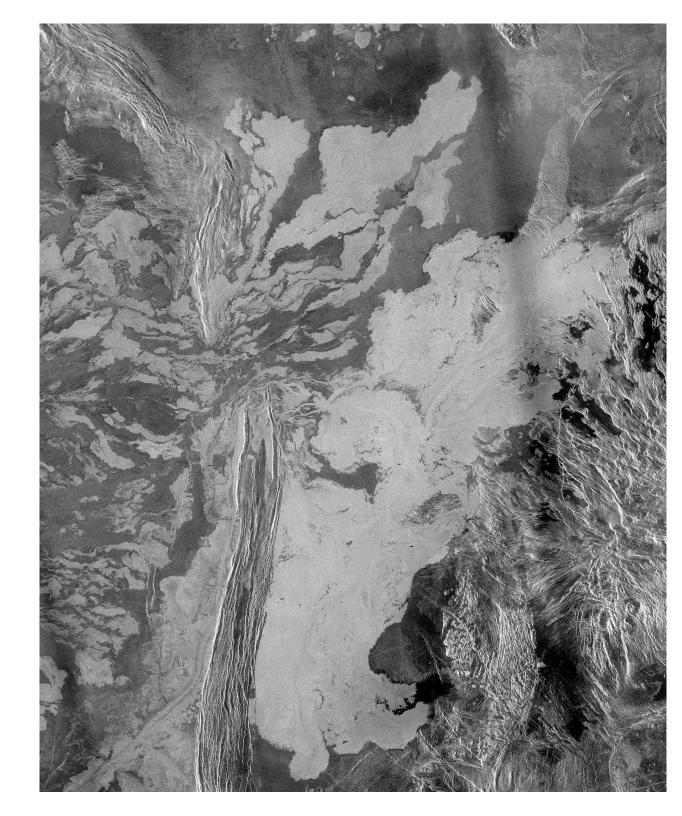
# slope

pancake domes Venus



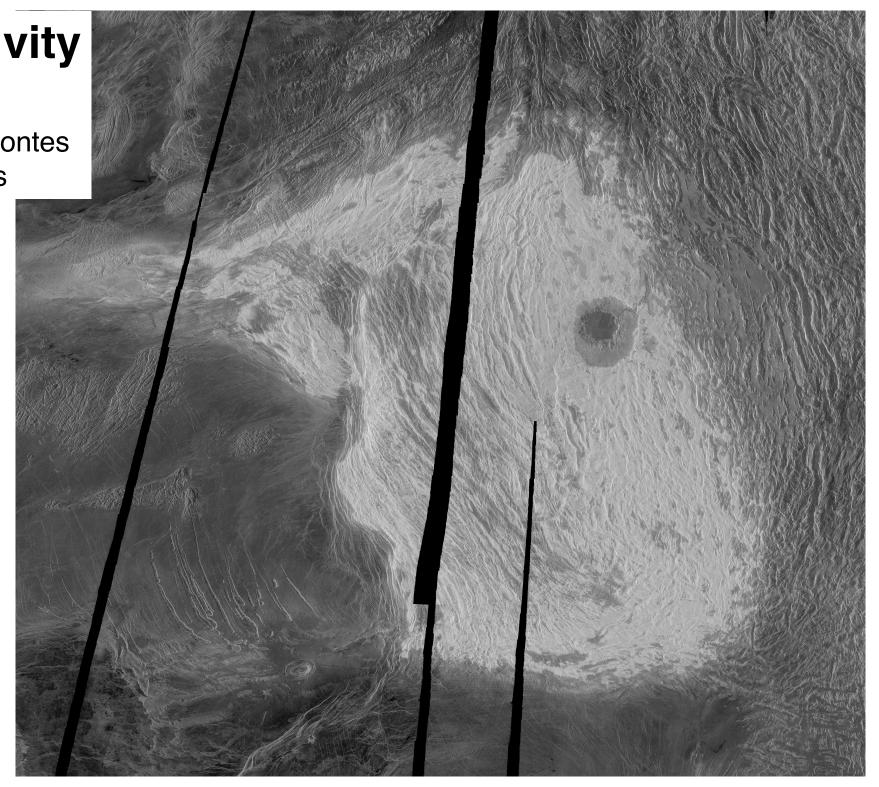
# roughness

lava flows Venus

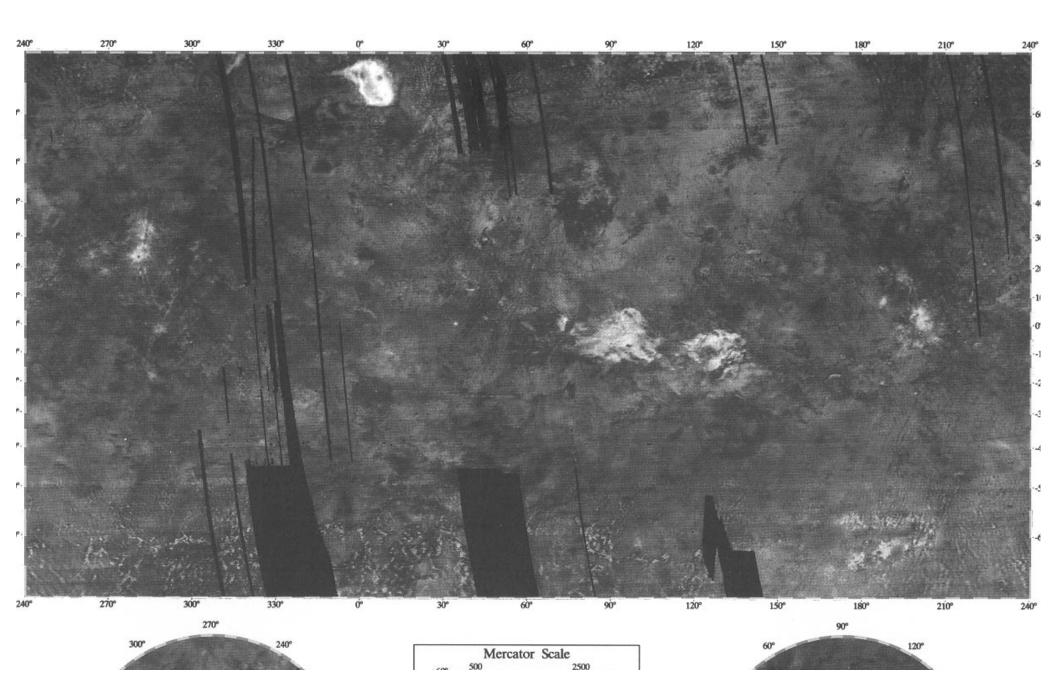


reflectivity

Maxwell Montes Venus



# reflectivity - Venus

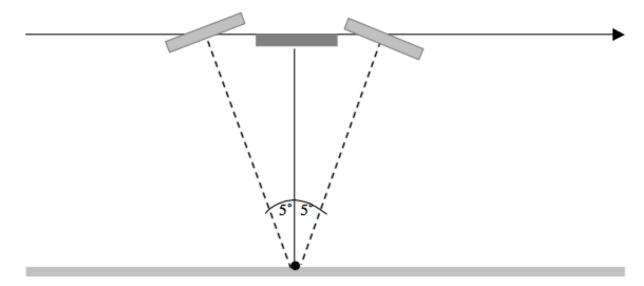


1) What is the illumination pattern for an aperture with a sign reversal at its center? What is P(0)? Is the function real or imaginary? Is the function symmetric or asymmetric?

The aperture is

$$A(y) = \begin{cases} 0 & |y| > \frac{L}{2} \\ 1 & 0 < y \le \frac{L}{2} \\ -1 & -\frac{L}{2} \le y < 0 \end{cases}$$

3) What is the theoretical azimuth resolution of a spotlight-mode SAR that can illuminate the target over a 10° angle as shown in the diagram below.



- 5) What is the ground-range resolution of side-looking radar with a pulse length of  $6x10^{-8}$  s and a look angle of  $45^{\circ}$ ?
- 6) (a) What is the period for a satellite in a circular orbit about the moon where the radius of the orbit is 1.9x10<sup>6</sup> m? The mass of the moon is 7.34x10<sup>22</sup> kg.
  - (b) You are developing a SAR mission for the moon. The length of your SAR antenna is 10 m. What minimum pulse repetition frequency is needed to form a complete aperture? The circumference of the moon is  $1.1 \times 10^7 \text{m}$ . You will need the orbital period from problem (a).

# Next Lecture SAR Interferometry InSAR